

DO NOW
 If $f(1) = 3$ and $f(n) = -2f(n-1) + 1$, find $f(5)$.

$f(2) = -2f(2-1) + 1$ $f(3) = -2f(3-1) + 1$
 $f(2) = -2f(1) + 1$ $f(3) = -2f(2) + 1$
 $f(2) = -2(3) + 1$ $f(3) = -2(-5) + 1$
 $f(2) = -6 + 1$ $f(3) = 11$
 $f(2) = -5$

$f(4) = -2f(4-1) + 1$ $f(5) = -2f(5-1) + 1$
 $f(4) = -2f(3) + 1$ $f(5) = -2f(4) + 1$
 $f(4) = -2(11) + 1$ $f(5) = -2(-21) + 1$
 $f(4) = -22 + 1$ $f(5) = 43$
 $f(4) = -21$

(b) $a_n = a_1 + d(n-1)$
 $a_1 = -5$ $a_n = -5 + d(n-1)$
 $d = 6$

(c) $f(k+1) = 2f(k) - 1$
 $f(1) = 3$

$f(2)$ $f(3)$
 $f(k+1) = 2f(k) - 1$ $f(2) = 2f(1) - 1$
 $f(1+1) = 2f(1) - 1$ $f(3) = 2f(2) - 1$
 $f(2) = 2(3) - 1$ $f(3) = 9$
 $f(2) = 5$

Feb 24-10:36 AM

Geometric Sequences - Explicit Form

- Determine if the sequence is geometric (Do you multiply or divide the same amount from one term to the next?)
- Find the common ratio (The number you multiply or divide)
- Create an explicit formula using:

$$a_n = a_1 \cdot (r)^{n-1} \quad \text{OR} \quad f(n) = f(1) \cdot (r)^{n-1}$$

$a_n = f(n)$ = the n^{th} term in the sequence
 $a_1 = f(1)$ = the first term in the sequence
 n = the term number
 r = the common ratio

Feb 22-10:06 AM

Sequence: {3, 6, 12, 24, 48, 96, ...}. Find an explicit formula.

First term (a_1) = 3 Common ratio (r) = 2

Explicit Formula
 Subscript Notation: $a_n = 3(2)^{n-1}$

Function Notation: $f(n) = 3(2)^{n-1}$

Feb 22-10:13 AM

Write an explicit rule for each sequence:

- 1, 10, 100, 1000, ...
- $\left\{1, \frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \dots\right\}$
- | | | | | | |
|--------|---|---|---|----|-----|
| n | 1 | 2 | 3 | 4 | ... |
| $f(n)$ | 2 | 4 | 8 | 16 | ... |

 $a_1 = 2$ $r = 2$ $a_n = 2(2)^{n-1}$
- 54, 18, 6, 2, ...
 $a_1 = 54$ $a_n = 54\left(\frac{1}{3}\right)^{n-1}$
 $r = \frac{1}{3}$

Feb 24-10:48 AM

Finding the n^{th} term of a Geometric Sequence

5) Find the 9th term given $a_1 = -15$ and $r = 3$
 $a_n = -15(3)^{n-1}$
 $a_9 = -15(3)^{9-1}$ $a_9 = -98,415$
 $a_9 = -15(3)^8$

6) Find the 10th term of the geometric sequence with $a_1 = \frac{1}{2}$ and $r = 4$

Feb 25-7:26 AM

Geometric Sequences - Recursive Form

Subscript notation
 a_1 = first term ; $a_n = r \cdot a_{n-1}$

Function notation
 $f(1)$ = first term ; $f(n) = r \cdot f(n-1)$

Feb 25-10:43 AM

Write a recursive function for each sequence:

1) 8, 24, 72, 216, ... $a_1 = 8; a_n = 3 \cdot a_{n-1}$
 $a_1 = 8$ $r = 3$

2)

n	1	2	3	4	...
$f(n)$	2	4	8	16	...

 $f(1) = 2$ $r = 2$ $f(1) = 2; f(n) = 2 \cdot f(n-1)$

3) 54, 18, 6, 2, ...
 $a_1 = 54$
 $r = \frac{1}{3}$ $a_1 = 54; a_n = \frac{1}{3} \cdot a_{n-1}$

Feb 25-10:47 AM

A geometric sequence is shown in the table below, where a_n represents the n th term of the sequence. What is the recursive formula for the geometric sequence?

a) $a_{n+1} = a_n^2$

b) $a_{n+1} = a_n + 3$

c) $a_{n+1} = 2a_n$

d) $a_{n+1} = 4a_n$

a_n	Value
a_1	1
a_2	4
a_3	16
a_4	64
a_5	216

Feb 25-10:48 AM

HOMEWORK

Workbook

p. 499 #1 - 3

p. 501 # 1 - 10

Feb 25-7:37 AM

7) Write a rule for the n th term of the geometric sequence 2, -8, 32, -128,.... Then find a_8 .

8) What is the fifteenth term of the sequence 5, -10, 20, -40, 80,....?

a) -163, 840 c) 81,920
 b) -81,920 d) 327,680

Feb 25-7:31 AM

9) In a geometric sequence $r = -2$ and $a_3 = 16$.

a. Find the value of a_1

b. Write the rule for the n th term of this sequence.

10) In a geometric sequence $r = 3$ and $a_2 = 12$.

a. Find the value of a_1

b. Write the rule for the n th term of this sequence.

Jan 27-2:29 PM