

Name: _____

Date: _____

CC Algebra

Recursive Sequence - Day 2

- 1) The table below represents the first 5 triangular numbers in a sequence graphically.

Figure in the Series	Triangular Number	Diagram
1 st	1	•
2 nd	3	• • •
3 rd	6	• • • • • •
4 th	10	• • • • • • • • • •
5 th	15	• • • • • • • • • • • • • • •

Part A

Write a recursive definition for finding the n^{th} term of this sequence.

Answer: _____

Part B

Use the definition written for Part A to determine the number of dots needed to form the 10th figure in the sequence?

Show your work.

Answer: _____ dots

- 2) Tyler gets a starting salary of \$22,600, with annual raises of \$800.

Part A

Write an explicit formula to model Tyler's salary after n years of employment when $n \geq 1$.

Answer: _____

Part B

Write an equivalent recursive definition for representing Tyler's salary.

Answer: _____

Part C

What will his salary be during his fourth year on the job?

Show your work.

Answer: \$ _____

- 3) Determine the first three terms of the given sequence using the recursive rule:

$$f(1) = 5 \text{ and } f(n + 1) = f(n)^2 - 1$$

Show your work.

Answer: _____

- 4) Given the sequence defined by the explicit formula $f(n) = 9 - 2(n - 1)$, where $n \geq 1$.

Part A

State the first 4 terms of this sequence.

Show your work.

Answer: _____

Part B

Rewrite the formula for this sequence using an equivalent recursive definition.

Show your work.

Answer: _____

- 5) Find the third term in the recursive sequence $f(k + 1) = 2f(k) - 1$, where $f(1) = 3$.

Show your work.

Answer: _____

- 6) Find the first four terms of the recursive sequence defined below.

$$f(1) = -3$$

$$f(n) = f(n - 1) - n$$

Show your work.

Answer: _____

- 7) When Myra started college, tuition was \$8,240 per semester. Each year, the tuition per semester increased by \$400.

Part A

Write an explicit formula to model the semester tuition cost after n years when $n \geq 1$.

Answer: _____

Part B

Write an equivalent recursive definition to represent the semester tuition cost.

Answer: _____

Part C

What was the cost of tuition per semester during her fourth year at college?

Show your work.

Answer: \$ _____

- 1) Part A: $f(1) = 1, f(n + 1) = f(n) + n$
Part B: 55 dots
 WORK SHOWN: $f(6) = f(5) + 6 = 21, f(7) = f(6) + 7 = 28, f(8) = f(7) + 8 = 36, f(9) = f(8) + 9 = 45, f(10) = f(9) + 10 = 55$
- 2) Part A: $S(n) = 22,600 + 800(n - 1)$;
Part B: $S(1) = 22,600$ and $S(n + 1) = 800 + S(n)$;
Part C: \$25,000
 WORK SHOWN: $S(4) = 22,600 + 800(3) = 25,000$
- 3) $5, -\frac{24}{25}, \frac{49}{576}$
- 4) Part A: 9, 7, 5, 3
 WORK SHOWN: $f(1) = 9 - 2(1 - 1) = \mathbf{9}, f(2) = 9 - 2(2 - 1) = \mathbf{7}, f(3) = 9 - 2(3 - 1) = \mathbf{5}, f(4) = 9 - 2(4 - 1) = \mathbf{3}$;
Part B: $f(1) = 9$ and $f(n + 1) = f(n) - 2, n \geq 1$
 WORK SHOWN: Arithmetic Sequence: $a = f(1) = 9, d = 7 - 9 = -2; f(n + 1) = f(n) - 2$
- 5) $f(3) = 9$
 WORK SHOWN: $f(k + 1) = 2f(k) - 1$ and $f(1) = 3; f(2) = 2f(1) - 1 = 2(3) - 1 = 5, f(3) = 2f(2) - 1 = 2(5) - 1 = 9$
- 6) -3, -5, -8, -12
 WORK SHOWN: $f(1) = \mathbf{-3}$ and $f(n) = f(n - 1) - n; f(1) = f(2 - 1) - 2 = -3 - 2 = \mathbf{-5}, f(3) = f(3 - 1) - 3 = -5 - 3 = \mathbf{-8}, f(4) = f(4 - 1) - 4 = -8 - 4 = \mathbf{-12}$
- 7) Part A: $T(n) = 8,240 + 400(n - 1)$;
Part B: $S(1) = 8,240$ and $S(n + 1) = 400 + S(n)$;
Part C: \$9,440
 WORK SHOWN: $S(4) = 8,240 + 400(3) = 9,440$