

DO NOW:

Solve for x:

$$x^2 - 6x = -x - 4$$

$$+x+4 \quad +x+4$$

$$x^2 - 5x + 4 = 0$$

$$(x-1)(x-4) = 0$$

$$x-1=0 \quad | \quad x-4=0$$

$$x=1 \quad | \quad x=4$$

$$\begin{array}{r} 4 \overline{) 5} \\ \underline{4} \\ 1 \end{array}$$

HW Answers

1. 2

2. 1

3. 4

4. 3

5. 2

6. 2

7. $y = x^2 + 4x - 5$

$y = x - 1$

Solutions

(1,0)

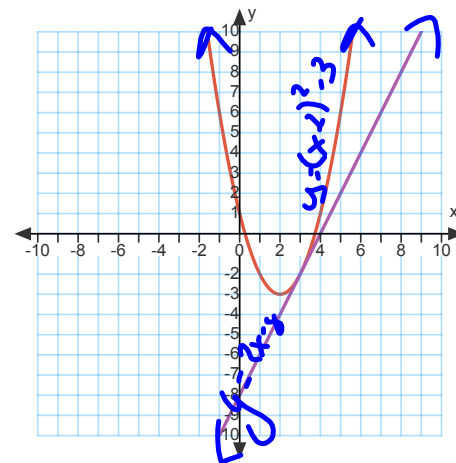
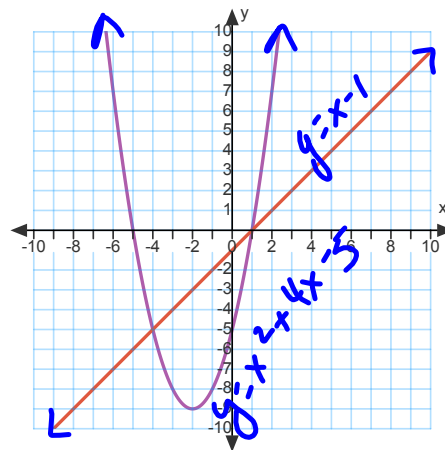
(-4, -5)

8.

(3,-2)

$y = (x - 2)^2 - 3$

$y = 2x - 8$



Quadratic-Linear Systems Algebraically

STEPS

- 1) Make sure that the quadratic equation is in standard form: $y = ax^2 + bx + c$**
- 2) Make sure that the linear equation is in slope-intercept form: $y = mx + b$**
- 3) Set the two equations equal to each other**
- 4) Solve the resulting quadratic equation using any method (factor or quadratic formula)**
- 5) Substitute the x-values into one of the equations to solve for the y-values**
- 6) Check your solutions**

Example 1

Solve the following system algebraically.

$$\begin{array}{r}
 y = x^2 + 3x + 2 \\
 2x + y = -4 \\
 \hline
 -2x \quad -2x \\
 \hline
 y = -2x - 4
 \end{array}$$

$$\begin{array}{r}
 x^2 + 3x + 2 = -2x - 4 \\
 +2x + 4 \quad +2x + 4 \\
 \hline
 x^2 + 5x + 6 = 0 \\
 (x+3)(x+2) = 0 \\
 x+3=0 \quad | \quad x+2=0 \\
 x=-3 \quad | \quad x=-2
 \end{array}$$

$x = -3$

$$\begin{array}{r}
 2x + y = -4 \\
 2(-3) + y = -4 \\
 -6 + y = -4 \\
 +6 \quad +6 \\
 \hline
 y = 2
 \end{array}$$

$x = -2$

$$\begin{array}{r}
 2x + y = -4 \\
 2(-2) + y = -4 \\
 -4 + y = -4 \\
 +4 \quad +4 \\
 \hline
 y = 0
 \end{array}$$

$(-3, 2)$ $(-2, 0)$

Quadratic

$$\begin{aligned}
 y &= x^2 + 3x + 2 \\
 2 &= (-3)^2 + 3(-3) + 2 \\
 2 &= 9 - 9 + 2 \\
 2 &= 2 \quad \checkmark
 \end{aligned}$$

Linear

$$\begin{aligned}
 2x + y &= -4 \\
 2(-3) + (2) &= -4 \\
 -6 + 2 &= -4 \\
 \checkmark \quad -4 &= -4
 \end{aligned}$$

Quadratic

$$\begin{aligned}
 y &= x^2 + 3x + 2 \\
 0 &= (-2)^2 + 3(-2) + 2 \\
 0 &= 4 - 6 + 2 \\
 0 &= -2 + 2 \\
 0 &= 0 \quad \checkmark
 \end{aligned}$$

Linear

$$\begin{aligned}
 2x + y &= -4 \\
 2(-2) + 0 &= -4 \\
 -4 &= -4 \quad \checkmark
 \end{aligned}$$

Example 3

Solve the following system algebraically.

$$y - x^2 = -2x + 1$$

$$y + 3 = x \rightarrow y = x - 3$$

$$\begin{array}{r} \cancel{x-3} = x^2 - 2x + 1 \\ \phantom{\cancel{x-3}} -x + 3 -x + 3 \\ \hline 0 = x^2 - 3x + 4 \end{array}$$

$$\begin{array}{r} \cancel{y - x^2} = -2x + 1 \\ \phantom{\cancel{y - x^2}} +x^2 +x^2 \\ \hline y = x^2 - 2x + 1 \end{array}$$

Discriminant

$$\begin{array}{l} b^2 - 4ac \\ (-3)^2 - 4(1)(4) \\ 9 - 16 \\ -7 \end{array}$$

No Solution